

Pole coordinates and shape of 30 asteroids

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Abstract. To obtain a statistically reliable sample of minor planets with known rotation axis orientation and axes ratios, a selection of photometric lightcurves sufficiently covered to give the elements needed for applying the computation methods of the rotational elements was made.

Using the data reported in the “Amplitude-longitude ($A - \lambda$) plot catalogue of asteroids” (Riccioli & Blanco 1995) as a starting point, the amplitude-magnitude (AM) method (Zappalà et al. 1983a) was adopted.

Due to the poor data available, it was possible to apply the (AM) method only to 30 asteroids. For more than half of these objects no previous determination of pole coordinates and shape exists in the literature.

Key words: asteroids

1. Introduction

The availability of a statistically reliable sample of asteroids with well-determined rotation axis orientation and axes ratios is essential for the statistical and theoretical modelling of their collisional evolution. The knowledge of the rotation axis distribution becomes more interesting in the case of the asteroid families, because it is possible to ascertain how the fragments of the parent body are distributed in space upon fragmentation. For these reasons, in the last years some parts of observational asteroid researches have been focused on the collection of photometric lightcurves with the aim of acquiring enough and qualified data to compute the pole coordinates and shape of the asteroids.

A long-term and intense photoelectric observational campaign is in progress at the Astronomy Institute of Catania University, in collaboration with Torino Astronomical Observatory, having as its main aim the integration of the observational data of the asteroids with few or incomplete lightcurves.

By means of a careful search in the literature for asteroid lightcurves and of those recorded in our observational campaign, an amplitude-longitude plot catalogue of asteroids was compiled (Riccioli & Blanco 1995). Using the data reported in this catalogue as a starting point, we utilized the amplitude-magnitude (AM) method (Zappalà et al. 1983a) based on the assumption of triaxial ellipsoid shape of the asteroid, rotating around the shorter axis. From the lightcurves, we obtain the magnitude V at the maximum of the lightcurve and the amplitude A , depending on the rotation axis orientation and on the shape of the asteroid, respectively. The ratio between the two greater axes of the approximating ellipsoid can be obtained from the plot ($A - \lambda$), if we have a continuous and good distribution in longitude of the observed amplitudes.

Due to the scarce availability of lightcurves from which the amplitude at suitable longitudes can be obtained, it was possible to apply the (AM) method only to 30 asteroids. Of these objects we report the observed and theoretical amplitude-longitude plots and the found values of the pole coordinates and of the axes ratios. For more than half the objects, this is the first determination of the rotation axis orientation and shape.

2. Photoelectric observations and reduction

To increase the observational data contained in the literature, mainly in the “Asteroid Photometric Catalogue” (Lagerkvist et al. 1987a) and its Updates (Lagerkvist et al. 1989, 1992), a long-term and intense photoelectric observational campaign was undertaken in collaboration with M. Di Martino and G. De Sanctis of Torino Astronomical Observatory. Besides the purpose of building lightcurves of the asteroids with observational constraints (Di Martino et al. 1994), its aim is to observe asteroids with few or incomplete lightcurves, preferably at suitable ecliptic longitudes to obtain ($A - \lambda$) plots with well distributed points in longitude.

The photoelectric observations, still in progress, have been carried out, since March 1992, with the 91-cm Cassegrain telescope at M.G. Fracastoro station

of Catania Astrophysical Observatory (since 28 October 1995 this has been the new name of Serra La Nave stellar station of Catania Astrophysical Observatory). In Table 1 of the “Amplitude-longitude ($A - \lambda$) plot catalogue of asteroids” (Riccioli & Blanco 1995), the date of the observational runs and the name of the observed asteroids are reported.

During the 23 runs of observations already made, each lasting on average ten nights, we have used the same instrumentation (photomultiplier, diaphragm, filters, etc...) and observing strategy (Di Martino et al. 1994). The transformation to the standard system was made by means of groups of standard stars, taken from Blanco et al. (1968) and Landolt (1973), usually observed every night on their passage at the meridian. Further information on the reduction and plotting procedure are reported in Di Martino et al. (1994).

3. Pole and shape determination

In order to determine the orientation of the rotational axis and the shape of the asteroid, we used the amplitude-magnitude (AM) method suggested by Zappalà (1981) and refined by Zappalà et al. (1983a), which is based on the assumed ellipsoidal shape of the asteroid (with semi-axes $a > b > c$) and on the relationships between the aspect angle, the lightcurve amplitude and the asteroid magnitude at the lightcurve maximum, all obtained in several oppositions (at least three). It is important to note that usually the real shape of asteroids is different from the ellipsoidal one and moreover the albedo is often not homogeneous over the entire surface. These discrepancies often lead to conflicting results especially when the data are few.

From the lightcurves, we obtain the magnitude V at the maximum of lightcurve and the amplitude A , depending on the rotation axis orientation and on the ratio of the maximum to minimum cross-sections of the asteroid, respectively.

If we assume the smaller axis c to be the asteroid rotation axis, the ratio between the two other axes, and subsequently their single values, can be obtained from the ($A - \lambda$) plot, if we have a continuous and good distribution in longitude of the observed amplitudes. The modelling curves were obtained using the least square method.

In some cases the extrema of the theoretical curves seem to be overestimated with respect to the observed values. This fact depends on the computing program that, in the absence of observed values at the longitudes of the maximum or the minimum, takes into account the slope of the ascending or descending branches.

From the axes ratios it is possible to obtain the value of the aspect angle (with an uncertain definition of the north or south pole) and hence the pole longitude.

Following Zappalà et al. (1990) suggestions, we have corrected the lightcurve amplitude for its dependence on the

phase angle, by means of the relationship $A(0^\circ) = \frac{A(\alpha)}{(1+m\alpha)}$ where $A(\alpha)$ is the observed lightcurve amplitude, α is the solar phase angle and m is a coefficient depending on the asteroid taxonomic class. The $V_0(1, \alpha)$ of each asteroid was computed adopting the value α_m , the arithmetic average of all phase angles.

In Table 1, for each asteroid, the references of the lightcurves used for the estimation of the V magnitude and for the construction of the ($A - \lambda$) plots are reported. The symbol before the author’s name is that used in the corresponding ($A - \lambda$) plots. Only lightcurves at least 90% covered were utilized. Due to the available lightcurves, their minimum number (at least three) necessary for applying the (AM) method and to their distribution in longitude, it was possible to compute the pole coordinates and the axes ratios only for 30 asteroids. In Fig. 1, using different symbols for different authors as indicated in Table 1, the ($A - \lambda$) plots of these asteroids are reported. The λ adopted values are the mean values computed over the duration of each lightcurve. The filled symbols indicate the observed values of the amplitude A , the empty ones the corresponding values at longitudes $\lambda + 180^\circ$, the continuous and dashed (in the case of two solutions) lines the theoretical curves.

4. Results

According to Zappalà & Knezevic (1984), the (AM) method for spin-vector determination allows us to obtain a preliminary indication of the rotational properties of the asteroid. One cannot derive the sense of rotation, and it is practically impossible to distinguish between two pairs of opposite pole solutions, unless the choice takes into account one’s stand on the smaller error or on the better fit with the theoretical plot. Notwithstanding this, we preferred to adopt the simple and fast (AM) method, particularly suitable in the case of a very large number of rotation axis and shape determinations.

Table 2 lists the average solar phase angle, the adopted maximum amplitude and the obtained values of the pole coordinates and of the axes ratios of the asteroids to which it was possible to apply the (AM) method. For many asteroids there are two pairs of solutions and it is usually difficult to reject one pair in favour of the other. When this occurs, the two solutions (the P_1 solution normally has a smaller error than the P_2 one) differ by about 180° in ecliptic longitude. Since the data do not distinguish between prograde and retrograde rotation about the same axis, every tabulated solution has a symmetric one with equal probability, which is not reported in the table. The choice between the prograde or the retrograde reported solution was made according to the solution given by the computation program. For some asteroids we obtain errors of the order 1 or 2 degrees that, compared to the few data from which the solution was obtained, appear reasonably low.

Table 1. References of the lightcurves used for the estimation of the V magnitudes and for the construction of the $(A - \lambda)$ plots. The symbol before the author's name is the same used in the corresponding $(A - \lambda)$ plots

<i>8 Flora</i>	
◆ Ahmad 1954	
◆ van Houten et al. 1958	
■ Veverka 1971	
● Di Martino et al. 1989	
▲ Harris and Young 1989	
<i>10 Hygiea</i>	
▲ Groenveld and Kuiper 1954	
● Vesely and Taylor 1985	
■ Lagerkvist and Williams 1987	
◆ Michalowski et al 1991	
◆ Blanco and Riccioli this paper	
<i>11 Parthenope</i>	
● van Houten 1962	
▲ Wood and Kuiper 1963	
■ Blanco et al. 1997	
<i>14 Irene</i>	
● Groenveld and Kuiper 1954	
◆ Wamsteker and Sather 1974	
◆ Scaltriti et al. 1978	
▲ Chang et al. 1981	
■ Blanco et al. 1997	
<i>19 Fortuna</i>	
● Wang Chuan-Jin and Liu Dum-Zhag 1965	
▲ van Houten et al. 1979	
■ Lupishko et al. 1981, 1989	
◆ Weidenschilling et al. 1987, 1990	
● Harris et al. 1992	
● Blanco et al. 1996	
<i>24 Themis</i>	
▲ Degewij et al. 1979	
● van Houten-Groeneveld et al. 1979	
■ Harris et al. 1989	
<i>36 Atalante</i>	
● Harris and Young 1980	
▲ Schober and Schroll 1982	
■ Di Martino et al. 1987	
<i>42 Isis</i>	
▲ Harris and Young 1979	
■ Debehogne et al. 1982	
● Vesely and Taylor 1985	
◆ Hainaut-Rouelle et al. 1995	
<i>48 Doris</i>	
● Harris and Young 1980	
■ Debehogne et al. 1982	
▲ Schober and Schroll 1982	
<i>66 Maja</i>	
■ Di Martino et al. 1990	
▲ Blanco and Riccioli this paper	
<i>69 Hesperia</i>	
■ Poutanen et al. 1985	
▲ Di Martino et al. 1987	
◆ Dotto et al. 1992	
● De Angelis and Mottola 1995	
● Hainaut-Rouelle et al. 1995	
<i>71 Niobe</i>	
● Lustig and Dvorak 1975	
▲ Barucci et al. 1985	
■ Harris and Young 1989	
<i>77 Frigga</i>	
■ Lagerkvist and Rickmann 1982	
● Zappalà et al. 1983b	
▲ Harris and Young 1989	
◆ Hainaut-Rouelle et al. 1995	
<i>108 Hecuba</i>	
■ Blanco et al. 1994	
<i>115 Thyra</i>	
◆ Chang et al. 1981	
● Scaltriti et al. 1981	
▲ Mc Cheyne et al. 1985	
■ Magnusson and Lagerkvist 1991	

A comparison between the values found by us and the ones by other authors, mainly computed by different methods, shows a certain agreement.

8 Flora

Even if the literature provides many lightcurves, we utilized one value of A by Ahmad (1954); van Houten et al. (1958); Veverka (1971), and Harris & Young (1989) and two by Di Martino et al. (1989), the only ones showing sure values of the amplitude and giving the magnitude V

at the maximum of the lightcurve, necessary to apply the (AM) method. Among the existing solutions of this puzzling asteroid the values by Gehrels & Owings (1962), by Zappalà et al. (1983b) and Hollis et al. (1987) give partial solutions. A complete solution is given by Di Martino et al. (1989) and De Angelis (1995). All the solutions are in good agreement with that given by us.

10 Hygiea

To compute the pole coordinate and shape, 8 values of the amplitude, well distributed in longitude, were

Table 1. continued

<i>121 Hermione</i>	<i>287 Nephthys</i>
● Di Martino et al. 1987	● Scaltriti and Zappalà 1979
◆ Hutton 1990	◆ Weidenschilling et al. 1990
■ Piironen et al. 1994	■ Blanco et al. 1996
▲ Blanco et al. 1996	
<i>150 Nuwa</i>	<i>334 Chicago</i>
● Di Martino 1984	■ Zappalà et al. 1989
▲ Blanco et al. 1996	● Weidenschilling et al. 1990
<i>161 Athor</i>	<i>372 Palma</i>
● Debehogne and Zappalà 1980	▲ Zappalà et al. 1983b
■ Carlsson and Lagerkvist 1983	■ Haupt 1985
▲ Harris and Young 1989	● Weidenschilling et al. 1990
<i>165 Loreley</i>	<i>337 Campania</i>
● Schober et al. 1988	● Tedesco 1979
■ Weidenschilling et al. 1990	■ Di Martino et al. 1994
▲ Harris et al. 1992	▲ Blanco et al. 1996
◆ Shevchenko et al. 1992	
<i>196 Philomela</i>	<i>386 Siegena</i>
● Yang et al. 1965	■ Zappalà et al. 1982
▲ Zappalà et al. 1983b	● Harris and Young 1989
◆ Erikson et al. 1991	
■ Licandro et al. 1994	<i>389 Industria</i>
<i>230 Athamantis</i>	● Haupt 1980
▲ Harris and Young 1980	▲ Magnusson and Lagerkvist 1991
■ Zeigler and Florence 1985	■ Lagerkvist et al. 1992
● Harris and Young 1989	
◆ Harris et al. 1992	<i>409 Aspasia</i>
<i>236 Honoria</i>	● Lagerkvist 1981
● Lagerkvist et al. 1987b	▲ Hanslmeier 1982
▲ Harris and Young 1989	■ Di Martino and Cacciatori 1984
■ Blanco et al. 1996	◆ Hainaut-Rouelle et al. 1995
	<i>624 Hektor</i>
	● Dunlap and Gehrels 1969
	■ Hartmann and Cruikshank 1978
	▲ Dahlgren et al. 1991
	◆ Hainaut-Rouelle et al. 1995

utilized. Our results are in agreement with the previous ones found by Michalowski et al. (1991); Erikson & Magnusson (1993) and Michalowski (1993), except for one solution, having the same longitude, but the β_0 value negative. Magnusson (1996) reports synthesis values, with an error of $\pm 10^\circ$, that differ from ours by the sign of the latitude of the P_1 solution.

14 Irene

The available six values of the amplitude A present an absence in correspondence with the longitude of the maximum. The only solution found in literature comes from

Bel'skaya et al. (1993) who reported only two values of the longitude with one that differs from the solution found by us.

19 Fortuna

The $(A-\lambda)$ plot of this asteroid too, even if with many determinations of the amplitude, presents few values at the maximum. Hansen (1977); Morrison (1977) and Lupishko et al. (1985) classify 19 Fortuna as a prograde asteroid. Our values of the pole coordinates and of the axes ratios substantially agree with the ones computed with different methods by Drummond et al. (1988, 1991); Magnusson

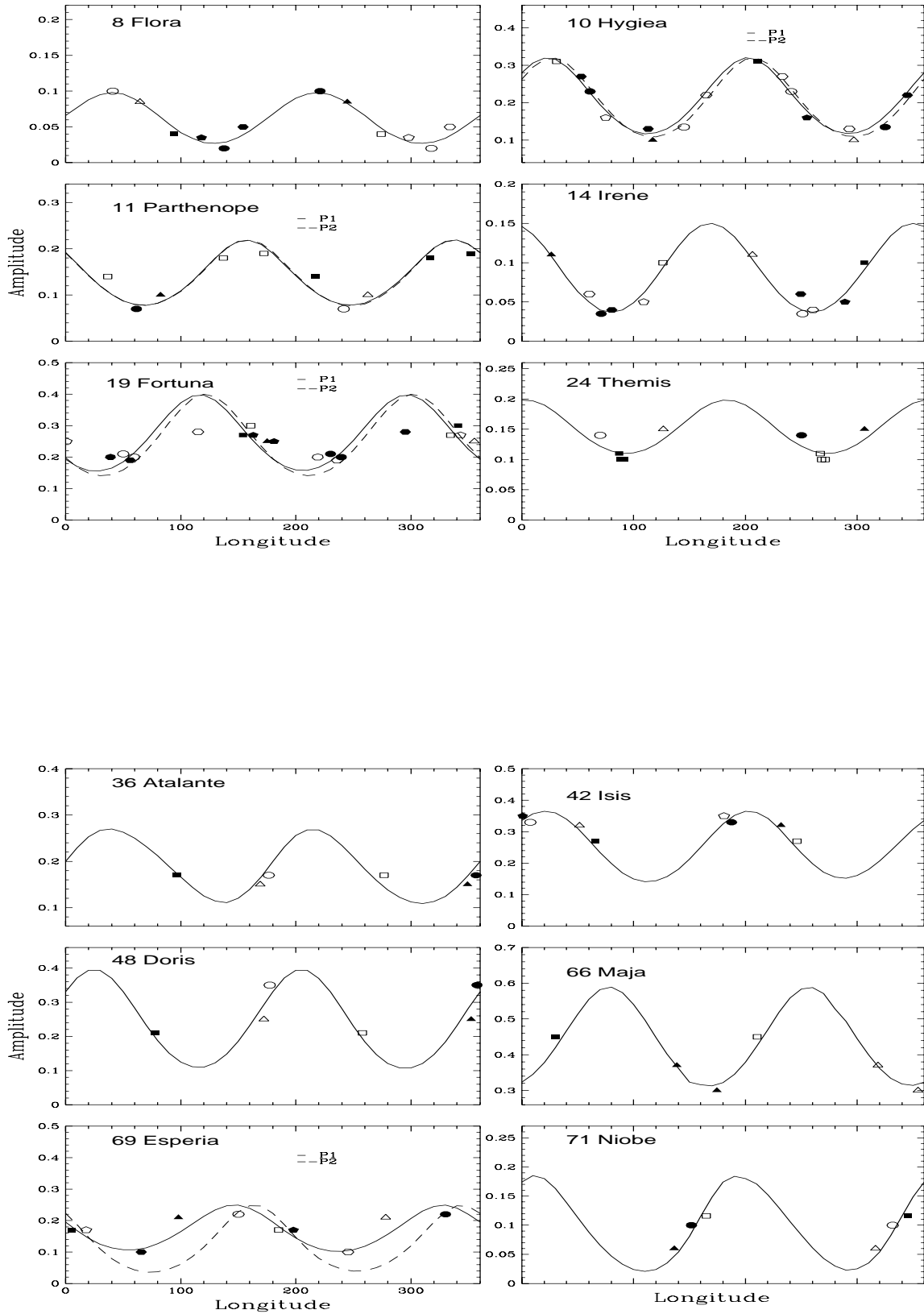


Fig. 1. Amplitude-longitude plots of the asteroid to which it was possible to apply the (AM) method. The filled symbols, as reported in Table 1, indicate the observed values of the amplitude A , the empty ones the corresponding ones at longitudes $\lambda + 180^\circ$, the continuous and (in the case of two solutions) dashed lines the theoretical curves

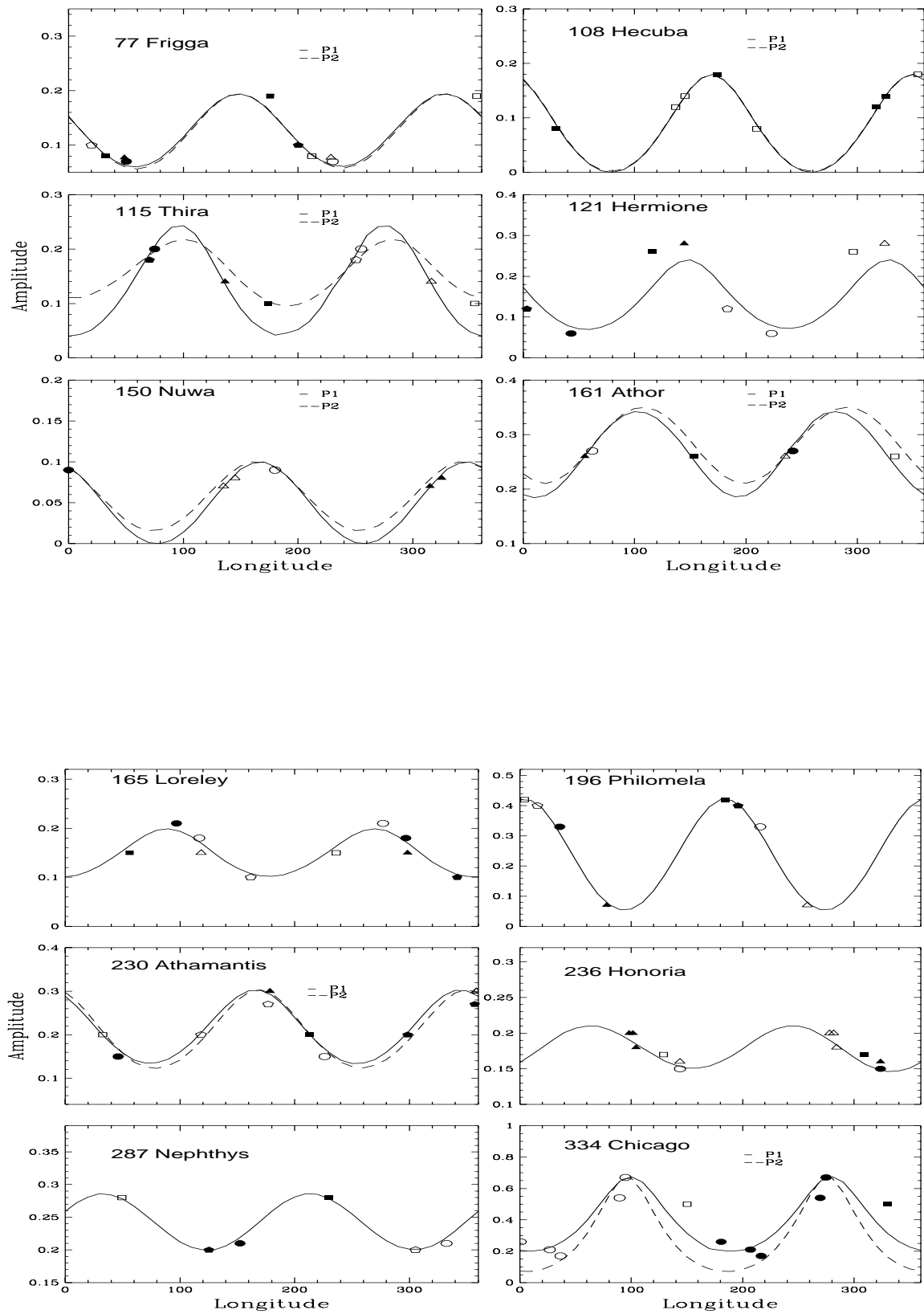


Fig. 1. continued

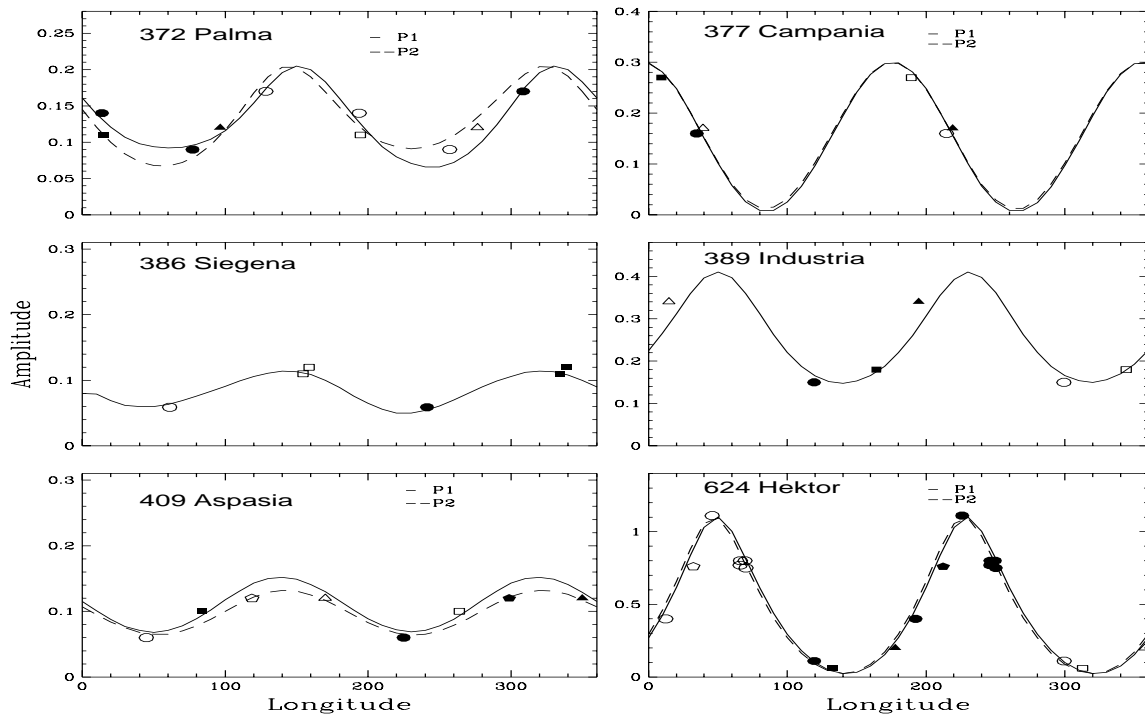


Fig. 1. continued

(1990) and De Angelis (1995). Only our a/b value is a little greater than the other ones. This discrepancy probably results from the overestimated extrema of the theoretical $(A - \lambda)$ plot.

69 Esperia

The five values found in literature are well distributed in longitude but show little variations in amplitude. Our pole coordinates differ from those by Velichko et al. (1989) and De Angelis & Mottola (1995), which are themselves in disagreement. The only existing axes ratio, reported by De Angelis & Mottola (1995), agrees with those found by us. Krugly & Velichko (1992) and Magnusson (1996) indicate that 69 Esperia is a prograde rotator.

115 Thyra

The four amplitude determinations, available for the $(A - \lambda)$ plot, are distributed in longitude only in an interval of 100° . The only value, among those found by us, that agrees with the existing ones published by Dotto et al. (1995), is a longitude value λ_0 .

121 Hermione

The available A values of the amplitude are well distributed in longitude. The only value of our solution that

agrees with those existing in the literature, reported by De Angelis (1995), is the value of the pole latitude β_0 .

196 Philomela

The four amplitude determinations utilized to build the $(A - \lambda)$ plot provide well determined extrema and one solution. The existing determinations by Michalowski (1992, 1993); Licandro et al. (1994); De Angelis (1995) and Magnusson (1996), substantially agree with the values of our solution. Except for De Angelis (1995), the other authors obtained two pole solutions that differ by about 180° . The values of the axes ratios are also consistent with ours.

334 Chicago

The six lightcurves utilized to obtain the A values are not well distributed in longitude. We obtain two solutions that both differ from the one by Michalowski (1993), the only one found in the literature. The λ_0 values of both solutions found by us are the only ones that agree with the solution by Michalowski (1993).

389 Industria

The $(A - \lambda)$ plot was built with only three determinations of the amplitude. The solution found by us is consistent with one of the two solutions published by Michalowski (1993).

Table 2. Asteroids to which it was possible to apply the ($A-M$) method. In the columns from left to right, the name of the asteroids, the average solar phase angle, the adopted maximum amplitude, the coordinates of the pole and the axes ratios are reported. When the computation method gives two pairs of solutions, the P_1 solution normally has a smaller error than the P_2 one. According to the (AM) method that always gives pairs of opposite solutions, every tabulated solution has a symmetric solution with equal probability

Asteroid	α_m	A_{\max}	$\lambda_0(P_1)$	$\beta_0(P_1)$	$\lambda_0(P_2)$	$\beta_0(P_2)$	a/b	b/c
8 Flora	15°	0 ^m 10	122° ± 3	37° ± 3			1.097	1.062
10 Hygiea	7	0.32	118 ± 1	44 ± 1	302 ± 19	-42 ± 19	1.343	1.144
11 Parthenope	10	0.22	73 ± 7	-51 ± 5	244 ± 21	-38 ± 21	1.225	1.208
14 Irene	10	0.15	90 ± 3	-34 ± 2			1.148	1.080
19 Fortuna	10	0.30	65 ± 17	49 ± 9	244 ± 16	48 ± 10	1.445	1.096
24 Themis	5	0.19	274 ± 33	52 ± 33			1.191	1.148
36 Atalante	10	0.27	119 ± 3	-19 ± 3			1.282	1.000
42 Isis	10	0.38	122 ± 1	-36 ± 1			1.419	1.000
48 Doris	7	0.40	113 ± 6	27 ± 11			1.445	1.000
66 Maja	9	0.55	162 ± 3	-50 ± 1			1.660	1.000
69 Esperia	9	0.24	70 ± 8	-42 ± 9	244 ± 27	-39 ± 27	1.247	1.250
71 Niobe	5	0.20	94 ± 1	-14 ± 1			1.202	1.345
77 Frigga	5	0.22	57 ± 4	39 ± 3	236 ± 12	-40 ± 12	1.224	1.010
108 Hecuba	5	0.18	259 ± 7	-6 ± 7	79 ± 1	13 ± 11	1.180	1.101
115 Thira	12	0.22	17 ± 9	-30 ± 12	178 ± 13	-35 ± 13	1.224	1.088
121 Hermione	7	0.28	60 ± 12	-42 ± 18			1.294	1.393
150 Nuwa	10	0.10	257 ± 13	1 ± 13	73 ± 9	-27 ± 68	1.097	1.015
161 Athor	19	0.34	209 ± 1	47 ± 1	1 ± 2	48 ± 2	1.367	0.850
165 Loreley	5	0.19	159 ± 18	-65 ± 18			1.191	1.274
196 Philomela	7	0.42	98 ± 1	-20 ± 6			1.472	0.914
230 Athamantis	12	0.23	60 ± 8	-51 ± 6	271 ± 17	-44 ± 17	1.318	1.195
236 Honoria	9	0.22	178 ± 14	-66 ± 14			1.225	1.142
287 Nephthys	5	0.29	99 ± 2	54 ± 1			1.306	1.207
334 Chicago	9	0.80	0 ± 14	-59 ± 9	198 ± 47	-46 ± 47	2.089	1.742
372 Palma	13	0.20	241 ± 12	7 ± 12	44 ± 15	78 ± 4	1.202	1.066
377 Campania	5	0.30	266 ± 7	0 ± 7	86 ± 4	3 ± 47	1.318	0.898
386 Siegena	7	0.12	236 ± 19	-14 ± 19			1.116	0.776
389 Industria	9	0.36	127 ± 15	-52 ± 10			1.393	1.245
409 Aspasia	10	0.14	73 ± 6	48 ± 4	216 ± 14	35 ± 14	1.137	1.080
624 Hektor	7	1.11	316 ± 3	+3 ± 8	147 ± 13	20 ± 13	2.779	1.000

624 Hektor

The A determinations taken from 10 lightcurves are well distributed in longitude. For this well studied asteroid, 11 authors reported pole coordinates and axes ratios values. We obtain two solutions substantially in agreement with those already published and whose mean value was reported by Magnusson (1996).

Of the other 19 objects no previous determination of rotation axis direction and shape has been found in the literature. To the greater part of these minor planets the (AM) method was applied at the minimum conditions of applicability: only with three amplitude determinations but well distributed in longitude. Nevertheless the use of the (AM) method in critical conditions of applicability does not necessarily mean that the results obtained are unreliable. Also to many of the presented asteroids, for which previous determinations exist in the literature, the (AM) method was applied with only three values of the amplitude, obtaining values in accordance with those al-

ready known.

The presented results are the first step in our research program. Even if they are in a preliminary form, we wish to publish them to permit their immediate use. The research continues with dedicated observational campaigns and search in the literature for new published data.

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