

The relativistic beaming model for active galactic nuclei

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Received May 23; accepted September 27, 1995

Abstract. — In this paper a list of 48 objects with superluminal motions is compiled, and some of their properties are discussed.

Key words: galaxies: jets-galaxies: active-quasars: general-BL Lacertae objects: general

1. Introduction

The relativistic jet model (Blandford et al. 1977; Marscher 1978; Blandford & Rees 1978; Blandford & Konigl 1979) has been proposed to describe the observed properties of variable extragalactic radio sources associated with the nuclei of galaxies, quasars and blazars. This hypothesis has found increasing observational support, the most striking being perhaps the measurements of superluminal velocities in many of the sources which could be resolved by VLBI (Porcas 1987; Ghisellini et al. 1993).

In this paper, we present a sample of objects with superluminal motion and discuss some of their properties associated with beaming model.

Through out the paper, $H_0 = 100$ km/s/Mpc, $q_0 = 0.5$.

2. The sample of superluminal sources and some statistical results

2.1. Sample

Columns 1 to 7 in Table 1 give the name, redshift, visual magnitude (m_v), radio flux (5 GHz) in Jy. Superluminal velocity (β_{app}), maximum optical polarization and references.

2.2. Statistical results

Based on a beaming model, the following relations hold:

$$f_\nu^{ob.} = \delta_\nu^{3+\alpha} f_\nu^{in.} \quad (1)$$

$$\beta_{app} = \beta_{in} \cdot \sin \theta / (1 - \beta_{in} \cdot \cos \theta) = \delta \cdot \sin \theta \cdot \beta_{in} / (1 - \beta_{in}^2)^{0.5} \quad (2)$$

where $f_\nu^{ob.}$ and $f_\nu^{in.}$ are, respectively, the observed and intrinsic (corrected) flux densities, δ_ν is the Doppler factor, θ is the angle of the jet to the line of sight, α is the spectral index.

For a single group of objects, we should expect

$$m^{in.} = 5 \log z + c_1 \quad (3)$$

and

$$f^{in.} = -2 \log z + c_2 \quad (4)$$

From which it follows:

$$m_v^{ob.} - 5 \log z = -2.5 (3 + \alpha) \log \delta_0 \quad (5)$$

$$\log f_\nu^{ob.} + 2 \log z = (3 + \alpha) \log \delta_\nu \quad (6)$$

In the case of a very small angle, θ , i.e. $\sin \theta \sim (1 - \beta_{in})^{-0.5}$, $\delta \sim \beta_{app}$ can be obtained, and we should expect (here $\alpha = 1.0$ and $\alpha r = 0.0$ are adopted)

$$m_v^{ob.} - 5 \log z = -10 k \log \beta_{app} + c_1 \quad (7)$$

$$\log f^{ob.} + 2 \log z = 3 \log \beta_{app} + c_2 \quad (8)$$

for the optical magnitude and radio flux density respectively, where k is related with δ_0 and β_{app} by

$$\delta_0 \sim \beta_{app}^k \quad (9)$$

When the linear regression method is used to fit the data, the expected results have been obtained

$$m_v^{ob.} - 5 \log z = -(3.35 \pm 0.81) \log \beta_{app} + 20.25 \pm 0.25 (N = 42) \quad (10)$$

$$\log f_R^{ob.} + 2 \log z = (2. \pm 0.23) \log \beta_{app} - 1.31 \pm 0.07 (N = 41) \quad (11)$$

with correlation coefficients being -0.48 and 0.54 , respectively, at a confidence level greater than 99%. N is the number of the considered objects.

3. Discussions and conclusions

Apparent superluminal motion is common among core dominated quasars (Cohen 1989), superluminal motion and blazar properties are often related (Impey 1987), and superluminal motion and core dominance parameter are also related (Ghisellini et al. 1993).

In this paper, 48 objects with superluminal motion are compiled. 23 of which are highly polarized (Popt. > 3%), 14 of which have low polarization (Popt. < 3%), and 3 of which, 0615+820, 0723+679, and 1040+123, are not polarized; 34 are core dominated, and 10 are lobe-dominated; two, 0415+379 and 0710+439, are galaxies, 11, 0235+164, 0454+844, 0716+714, 0735+178, 0851+202, 1101+384, 1749+701, 1803+784, 1807+698, 2007+777, and 2200+420, are BL Lac objects. 3 objects, 0153+744, 0235+164, and 1807+698, are not included in some of our discussions, the correlations of $\log f_r + 2 \log z - \log \beta_{\text{app}}$, $m^{\text{ob.}} - 5 \log z - \log \beta_{\text{app}}$, $\log \beta_{\text{app}} - \log z$, and $\log R - \log \beta_{\text{app}}$ for instance. 0235+164 and 0153+744, are candidates for gravitational lensing (Kühr & Schmidt 1990; Surdej et al. 1992), their apparent superluminal motion may come from the effect of the gravitational lens. As to 1807+698, its optical Doppler factor is $\delta_o = 1.24$; after consideration of its Doppler factor it fits the Hubble relation very well (Xie et al. 1993; Fan et al. 1993); its radio Doppler factor calculated from SSC model is $\delta_R = 0.36$ (Madau et al. 1987). This means the Doppler factor of 1807+698 is very small, but its average apparent superluminal velocity is very high, $\beta_{\text{app}} = 7.7c$. Obviously, it does not obey the condition: $\delta \sim \beta_{\text{app}}$. As listed in Table 1, many objects have several determinations of their superluminal velocities. The velocity used to analyse is the average velocity in these cases.

3.1. Superluminal motion and beaming model

For the observations, we find $\log f_r = -(0.13 \pm 0.03) \log z + c$, $m = (2.27 \pm 0.16) \log z + c$ (see Figs. 1 and 2), which do not fit the Hubble relations: $\log f_r = -2 \log z + c$, $m = 5 \log z + c$. This is usually explained as duo to the fact that the emissions are strongly enhanced by the Doppler effect (Blandford & Konigl 1979; Worrall 1986; Fan et al. 1993). If so, we should expect that the corrected magnitude and radio flux density fit the Hubble relations well. The corrections can be expressed as Eqs. (7) and (8) in the case of small angles. From the data, the expected results have been obtained:

$$m_v^{\text{ob.}} - 5 \log z = -(3.35 \pm 0.81) \log \beta_{\text{app}} + 20.25 \pm 0.25,$$

$\log f^{\text{ob.}} + 2 \log z = (2. \pm 0.23) \log \beta_{\text{app}} - 1.31 \pm 0.07$ with correlation coefficients being -0.48 and 0.53 at a confidence level greater than 99% (see Figs. 3 and 4). Comparing Eq. (7) and the statistical result, one finds

$$\delta_0 \sim \beta_{\text{app}}^{1/3},$$

which means the enhancement of optical luminosity is associated with the superluminal motion.

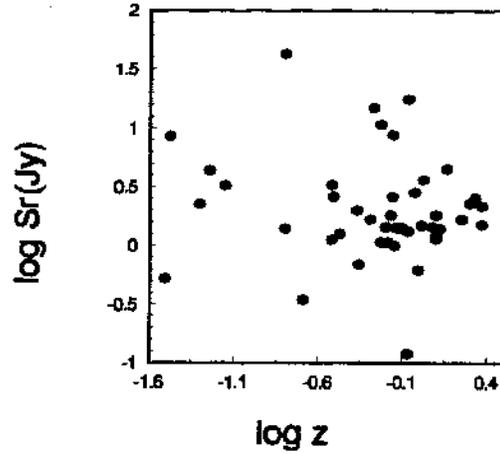


Fig. 1. Relation of radio flux density (5 GHz) and redshift

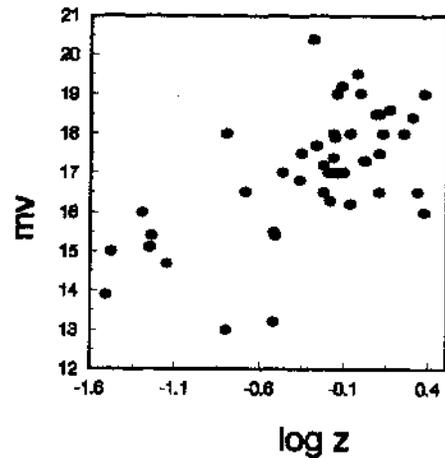


Fig. 2. Relation of visual magnitude (m_v) and redshift

3.2. Superluminal motion and radio luminosity and redshift

Cruz-Gonzalez & Carrillo (1991) supposed $\gamma_{\text{jet.}} \approx \beta_{\text{app}}$ and got $\gamma_{\text{jet.}} \sim L_{10\text{GHz}}^{0.28}$ for 30 objects.

From the data in the present paper, we have

$$\log \beta_{\text{app}} = 0.143 \log L_r - 4.35$$

with a correlation coefficient being 0.536 at a confidence level greater than 99% (see Fig. 7), which is consistent with the Cruz and Carrillo's result. It suggests that the radio emission is strongly enhanced by the Doppler effect. This statistical result also shows that the superluminal motion is associated with the redshift as

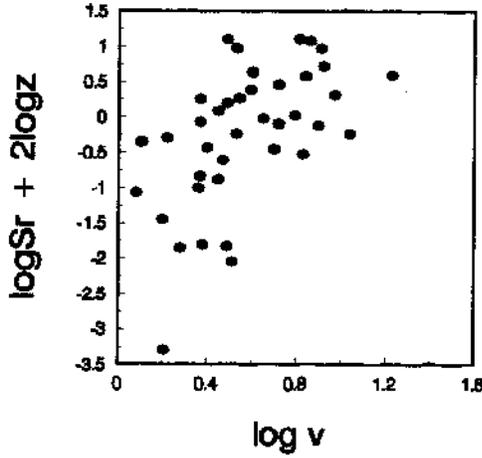


Fig. 3. Relation of $\log S_r + 2 \log z$ and superluminal velocity

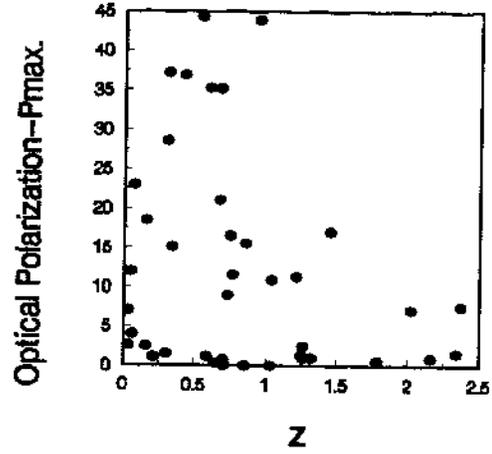


Fig. 5. Relation of optical polarization and redshift

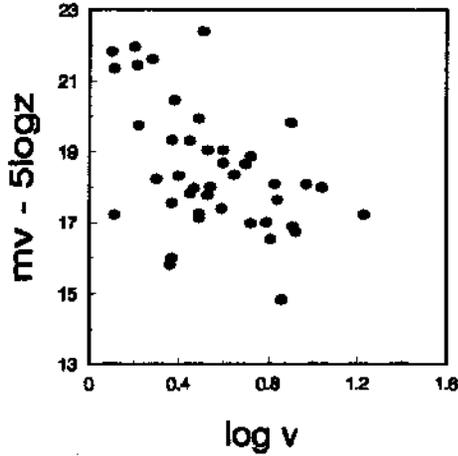


Fig. 4. Relation of $m_v - 5 \log z$ and superluminal velocity

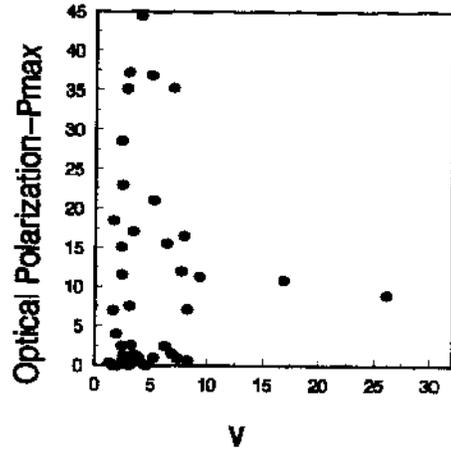


Fig. 6. Relation of optical polarization and superluminal velocity

$\log \beta_{app} = (0.22 \pm 0.01) \log z + 0.61 \pm 0.001$ with a confidence level greater than 99% (see Fig. 8): this means that distant objects have a stronger Doppler effect. This correlation may come from the fact that $\log L_r$ is closely associated with the redshift and $\log L_r$ is correlated with the superluminal velocity. This can be confirmed if we use Padovani's method (Padovani 1992) to deal with the relevant data.

If γ_{ij} is the correlation coefficient between x_i and x_j , in the case of three variables the correlation between two of them, excluding the effect of the third one, is (Padovani 1992)

$$\gamma_{12,3} = \frac{\gamma_{12} - \gamma_{13}\gamma_{23}}{(1 - \gamma_{13}^2)^{1/2}(1 - \gamma_{23}^2)^{1/2}}$$

From the data we find that the correlation coefficient between superluminal velocity and redshift, γ_{v_z, L_r} , excluding the effect of radio luminosity, L_r , is 0.132. The result means there is nearly no correlation between superluminal velocity and redshift: the obtained correlation is only from

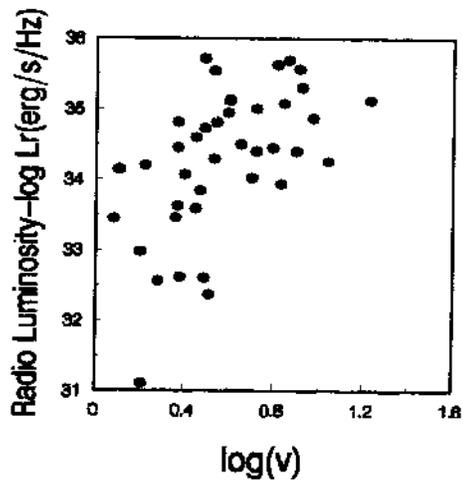


Fig. 7. Relation of radio flux and superluminal velocity

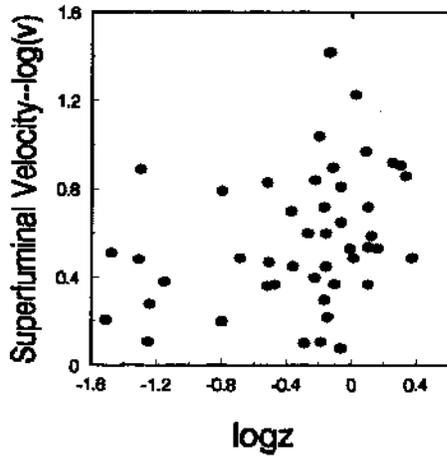


Fig. 8. Relation of superluminal velocity and redshift

an effect of the correlation (at level greater than 99%) between radio luminosity and redshift and superluminal velocity.

3.3. Polarization

23 of the 48 superluminal objects are highly polarized. Figure 5 shows that objects with a lower redshift have a higher polarization than those with higher redshifts, and Fig. 6 shows that objects with lower superluminal velocity have higher polarizations than those with higher velocity. That is why BL Lac objects have higher polarization and lower superluminal velocity than quasars. Figure 9 shows that objects with higher radio luminosity have lower polarization. Figure 10 shows that a higher polarization is associated with a high ratio of radio to optical luminosity- $\log L_r/L_0$, in agreement with Impey's result (Impey 1987). Figure 11 confirms Wills' result that polarization is associated with the core dominance (Wills 1989).

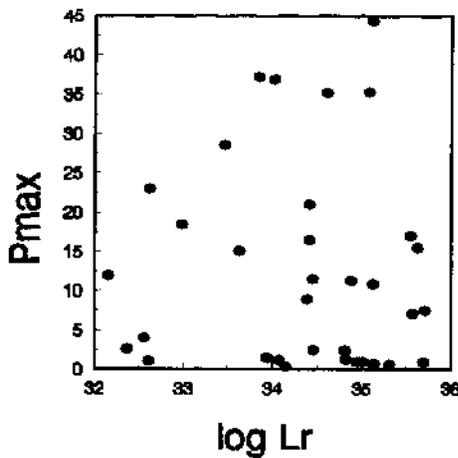


Fig. 9. Relation of optical polarization and radio flux

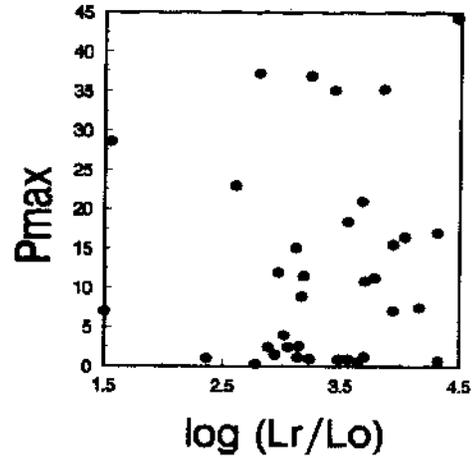


Fig. 10. Relation of polarization and ratio of radio to optical flux

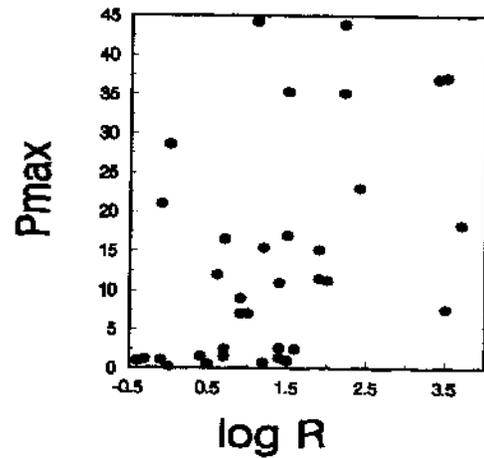


Fig. 11. Relation of optical polarization and core dominance parameter

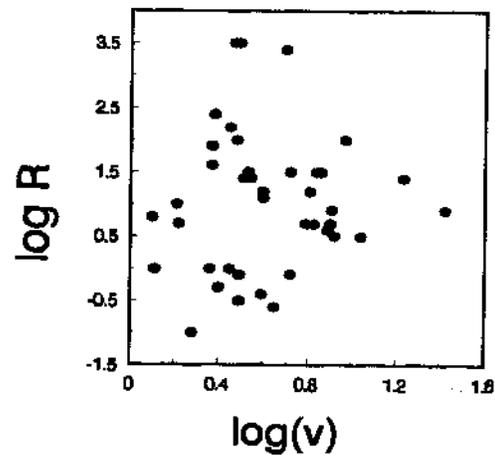


Fig. 12. Relation of superluminal velocity and core dominance parameter

Table 1. Objects with superluminal motions

Table 1. Objects with superluminal motions

Name (1)	Z (2)	m_v (3)	β_{app}/c (4)	f_R (5)	P_{MAX} (6)	Refs. (7)
0016+731	1.781	18.0	8.3	1.65	0.6	G93,S93
0106+013	2.017	18.39	8.2	2.28	7.1	Im88,V91,S93
0153+744	2.34	16.0	1.3	1.52	1.6	W87,W92,S93
0212+735	2.387	19.0	3.9	2.2	7.6	W92,W87,S93, Sc93
0234+285	1.21	18.5	9.3	1.44	11.3	S93,D94
0235+164	0.94	19.5	30.	2.85	43.9	W92,R93,Im87,S93
0333+321	1.26	17.5	4.8	1.8*	1.0	W92,P87,Wu92,Im87 S87
0415+379	0.049		3.0			P87,Wu92
0430+052	0.033	15.0	2.15	8.44	2.6	Pa87,K81,S87,S93 H87,P87,Im87
0454+844	0.16	18.0	1.6	1.39	18.4	P87,G93,B89,S93
0615+820	0.71	19.0	1.1	1.0	0.0	W87,W92,S93 G93
0710+439	0.518	20.4	1.25	1.67		G93,S93
0716+714	0.3	13.2	2.3	1.12	23.6	W87,G93,S93
0723+679	0.846	18.0	4.8	1.32	0.0	W92,W87,S93 S87,H87
0736+178	0.424	16.8	2.8	1.99	36.9	S87,M87,P87,S91,S93 G93
0836+710	2.16	16.5	6.2	2.59	1.0	W87,S93 R93
0850+581	1.322	18.0	3.9	1.39	<1.	K81,P87,S93,La87
0851+202	0.306	15.4	3.18	2.62	37.2	S91,S93,Wu92 P87
0906+430	0.669	18.0	8.6	1.80	21.0	S93,G93,P87 Wu92
0923+392	0.699	17.9	3.5	8.73	0.8	Sh87,W92,P87,S93 Sc93, Wu92
1038+528	0.678	17.4	2.0			W92,Im87
1039+81	1.26	16.5	2.5	1.14	2.5	W87,S93 G93
1040+123	1.03	17.3	3.1	1.47	0.0	W92,P87,S93
1101+384	0.031	13.9	1.36	0.53		R93,F94
1137+060	0.652	16.3	1.3	1.06	0.3	W92,P87,S93
1150+812	1.25	18.5	3.5	1.18	1.3	W87,Wu92,S93
1156+295	0.729	17.0	26.1	1.4	9.0	F93,G93,A80 G93
1222+216	0.435	17.5	1.4	0.69		P87

*: $S_{10\text{ GHz}} = 0.12\text{ Jy}$

Name (1)	Z (2)	m_v (3)	β_{app}/c (4)	f_R (5)	P_{MAX} (6)	Refs. (7)
1226+023	0.158	13.0	5.1	42.85	2.5	Z87,Im87,S93 S87,B87,W87
1259-055	0.598	17.7	2.0	14.96	44.3	V91,A80,B87,S93 S93,H87,U87
1641+399	0.595	16.5	9.5	10.81	35.3	A80,W92,B87,S93 P87,Kr93,H87
1642+690	0.751	19.2	7.9	1.39	16.5	K81,P87,S93
1721+343	0.206	16.5	3.1	0.35*	1.1	P87,W92,Wu92,Im87
1749+701	0.77	17.0	2.35	1.45	11.5	S91,S93,G93
1803+784	0.684	17.0	1.5	2.64	35.2	S91,M85,Sc93 S93,G93
1807+698	0.06	16.0	6.0	2.26	12.0	S91,L87,S93
1830+285	0.594	17.2	2.5	1.06	1.2	S93,G93
1845+797	0.057	15.4	1.9	4.38	4.0	K81,S93,P87,A80
1901+319	0.635	17.0	1.4	1.43		P87,Si87, S87,B87
1928+738	0.302	15.5	9.1	3.34	1.5	W87,P87,S87 Wu92,S93
1951+498	0.846		1.2	0.12*		P87,Wu92
1957+405	0.056	15.1	1.3			Kr93,V91,
2007+777	0.342	17.0	2.32	1.26	15.1	S91,K90,G93,S91,S93
2200+420	0.07	14.7	1.8	3.27	23.0	S93,H87,F93,S93 S87,G93
2223-052	1.454	18.6	3.35	4.51	17.0	S91,S83G93,S93
2230+114	1.037	17.3	18.	3.61	10.9	W92,P87,S93 D94,Im87
2233-148	0.976	19.0	3.35	0.61		V92,V91,G93
2251+155	0.857	16.2	8.8	17.42	15.5	C77,W92,P87, S93,Pa87

References to Table 1

- A80: Angel & Stockman (1980) B87: Brown (1987)
B88: Burbidge & Hewitt (1989) C77: Craine (1977)
D94: Dondi & Ghisellini (1994) F93: Fan et al. (1993)
F94: Fan et al. (1994) G93: Ghisellini et al. (1993)
H93: Hough et al. (1993) H87: Hough & Readhead (1987)
Im87: Impey (1987) Im88: Impey & Tapia (1988)
K93: Krichbaum et al. (1993a) K81: Kuhr et al. (1981)
Kr93: Krichbaum et al. (1993b) L87: Lind (1987)
La87: Lawrence et al. (1987) M87: Makino et al. (1987)
M85: Moles et al. (1985) P87: Porcas (1987)
Pa87: Pauling-Toth (1987) R93: Reich (1993)
S87: Simon et al. (1987a) S91: Stickel et al. (1991)
S83: Stocke et al. (1983) S87: Simon et al. (1987b)
Si87: Simon et al. (1987b) Sc93: Schalinski et al. (1993)
U87: Unwin (1987) V91: Veron & Veron (1991)
V92: Veron & Veron (1992) W87: Witzel (1987)
W92: Wills et al. (1992) Wu92: Wu et al. (1992)
Z87: Zensus (1987)

3.4. Core dominance parameter

If the extended emission of radio sources is unbeamed, while the flux of the core is enhanced by beaming, the flux ratio R of the core to the extended component should be a beaming indicator (Scheuer & Readhead 1979), or R indicates the orientation of the emission (Orr & Brown 1982). A correlation is then expected between R and the Doppler factor, δ .

Ghisellini et al. (1993) obtained a significant correlation (at the 99.8% level) between R and δ and a multiple correlation analysis shows in fact that R is still correlated with δ at the 98.8% level even when the effect of the core flux is subtracted, which gives confidence that the core dominance parameter is indeed a beaming indicator.

The measured superluminal velocity and the values of δ derived from the SSC argument are compared for 46 sources: a significant correlation (99.7% level) between the two quantities is obtained and is shown in Fig. 3 (Ghisellini et al. 1993). Obviously, we can expect that the core-dominated objects have a high superluminal velocity. This seems to be true (see Fig. 12). From the data in Table 1, we see that objects with higher redshifts tend to have a larger core dominance parameter, which suggests that distant objects tend to have a beaming effect. This is also consistent with the results that core-dominated quasars have a smaller viewing angle with respect to the line of sight ($\phi = 8.5 \pm 1.7$) and a stronger Doppler effect ($\log \delta = 0.79 \pm 0.09$) than BL Lac objects ($\phi = 14.0 \pm 2.5$, $\log \delta = 0.49 \pm 0.13$), lobe-dominated Quasars (LDQ) ($\phi = 25.1 \pm 6.4$, $\log \delta = 0.09 \pm 0.26$) and galaxies ($\phi = 40.5 \pm 8.1$, $\log \delta = 0.04 \pm 0.09$) (Ghisellini et al. 1993).

4. Conclusions

From the above analyses, we can come to the following conclusions. Superluminal motion and beaming effect are, to some extent, the same thing: They are related with radio luminosity, redshift, and the core dominance parameter; the optical Doppler factor is related with the superluminal velocity; polarization is associated with redshift, superluminal motion, ratio of radio to optical luminosity, and core dominance parameter; the core dominance parameter is an indicator of the orientation of the emission; probably most of the distant objects are beamed.

Acknowledgements. We thank an anonymous referee for his/her significant suggestions. This work is supported by the National Natural Science Foundation of China and the Natural Science Foundation of Guangdong Province (940557).

References

Angel J.R.D., Stockman H.S., 1980, *ARA&A* 18, 321
Blandford R.D., Konigl A., 1979, *ApJ* 232, 34

Blandford R.D., Rees M., 1978, in *Proc. Pitt. Conf. on BL Lac objects*. In: Wolfe A.M. (ed.). Pitt., Univ. of Pitt., 328
Blandford R.D., et al., 1977, *Nat* 211, 468
Brown I.W., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 129
Burbidge G., Hewitt A., 1989, in *BL Lac objects*. In: Maraschi L., Maccacaro T. & Ulrich M.-H. (eds.). Berlin: Springer, 412
Cohen M.H., 1989, in *BL Lac objects*. In: Maraschi L., Maccacaro T. & Ulrich M.-H. (eds.). Berlin: Springer, 13
Crain E.R., 1977, *A handbook of Quasistellar and BL Lac objects*. Pattchart Publishing House, Tucson, Ariz, Vol. 56, 63
Cruz-Gonzales I., Carrillo R., 1991, in *Variability of Blazars*. In: Valtaoja E. & Valtonen M. (eds.). Cambridge: Sydney, 256
Dondi L., Ghisellini G., 1995, *MNRAS* 273, 583
Fan J.H., et al., 1993, *ApJ* 415, 113
Fan J.H., et al., 1994, *A&AS* 105, 415
Ghisellini G., et al., 1993, *ApJ* 407, 65
Hough D.H., et al., 1993, *MPIfR*, Preprint Ser. No. 502
Hough D.H., Readhead A.C., 1987, in *Superluminal Radio Sources*. In: A. Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 114
Impey C.D., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 233
Impey C.D., Tapia S., 1988, *ApJ* 333, 666
Krichbaum T.P., et al., 1993a, *MPIfR*, Preprint Ser. No. 502
Krichbaum T.P., et al., 1993b, *MPIfR*, Preprint Ser. No. 508
Kuhr H., Schmidt D.A., 1990, *AJ* 99, 1
Kuhr H., Witzel A., Pauliny-Toth I.I.K. and Nauber U., 1981, *A&AS* 45, 367
Lind K.R., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 180
Lawrence C.R., et al., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 260
Madau M., Ghisellini G., Persic M., 1987, *MNRAS* 224, 257
Makino F., 1987, *ApJ* 313, 662
Marscher A.P., 1978, *ApJ* 219, 392
Moles M., et al., 1985, *ApJS* 58, 255
Orr M.J.L., Brown I.W.A., 1982, *MNRAS* 200, 1067
Padovani P., 1992, *A&A* 256, 399
Porcas R.W., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press 12
Pauliny-Toth I.I.K., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 55
Reich W., et al., 1993, *MPIfR*, Preprint Ser. No. 507
Schalinski C., et al., *MPIfR*, Preprint Ser. No. 502
Scheuer P.A.G., Readhead A.C.S., 1979, *Nat* 277, 182
Shafber D.B., Marscher A.P., 1987, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 67
Simon R.S., et al., 1987a, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 155
Simon R.S., et al., 1987b, in *Superluminal Radio Sources*. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 72

- Stickel M., et al., 1991, ApJ 374, 431
Stoche J.T., et al., 1983, ApJ 297, 458
Surdej J., et al., 1992, ESO Sci. Prep. No. 898
Unwin S.C., 1987, in Superluminal Radio Sources. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 34
Veron-Cetty M.-P., Veron P., 1992, Observatoire de Haute Provence, Pre-Publication No. 71
Veron-Cetty M.-P., Veron P., 1991, ESO Sci. Rep. No. 10
Witzel A., 1987, in Superluminal Radio Sources. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 83
Wills B.J., et al., 1992, ApJ 398, 454
Wills B.J., 1989, in BL Lac objects. In: Maraschi L., Maccacaro T. & Ulrich M.-H. (eds.). Berlin: Springer, 109
Worrall D.M., 1986, ApJ 303, 589
Wu S.Y., Quirrenbach Witzel A., 1992, Chinese Sci. Ser. A 7, 743
Xie G.Z., et al., 1993, A&A 278, 6
Zensus J.A., 1987, in Superluminal Radio Sources. In: Zensus A. & Pearson T.J. (eds.). Cambridge Univ. Press, 26